

FOURTH SEMESTER B.A. DEGREE EXAMINATION, APRIL 2018

(CUCBCSS—UG)

Economics

ECO 4B 05—QUANTITATIVE METHODS FOR ECONOMIC ANALYSIS—II

Time : Three Hours

Maximum : 80 Marks

Use of Calculator is permitted.

Part A

*Answer all the questions.*1. $\lim_{x \rightarrow 4} \frac{x^2 - 16}{x - 4}$ is :

- (a) 8. (b) 4.
(c) 6. (d) 0.

2. The derivative of $y = 5x^4$ with respect to x is :

- (a) $20x^3$. (b) $12x^4$.
(c) $20x^5$. (d) $4x^3$.

3. Marginal function is :

- (a) Ratio of total function and price. (b) Product of total function and x .
(c) Derivative of the total function. (d) Product of average function and x .

4. For the demand curve $x = 75 - 5p$, the price elasticity of demand at $p = 3$ is :

- (a) 2. (b) $\frac{3}{4}$.
(c) 1. (d) $\frac{1}{4}$.

5. The average which is commonly used in index number is :

- (a) A.M. (b) G.M.
(c) H.M. (d) Mode.

6. In Laspeyre's index number, the weight is

- (a) Current year quantity. (b) Base year quantity.
(c) Current year price. (d) Base year price.

Turn over

(12 x ½ = 6 marks)

Part B (Very Short Answer Questions)

Answer any ten questions.

13. Find the derivative of $y = x^3 + 2x^2 + 6$ with respect to x . $\frac{dy}{dx} = 3x^2 + 4x$

14. Define marginal revenue function.

15. Define continuity of a function ?

16. Define index numbers.

17. What is meant by BSE SENSEX ?

18. Define Paasche's index number.

19. What are the sources of vital statistics ?
20. Define specific death rate.
21. Define sex ratio.
22. Define sample space.
23. Define equally likely events.
24. An unbiased die is thrown two independent times. Given that the first throw resulted in an odd number. Find the probability that the sum obtained is 6.

(10 × 2 = 20 marks)

Part C (Short Essay Questions)

Answer any six questions.

25. Differentiate $\frac{(3x+1)^2}{x-2}$ with respect to x .
$$\frac{9x^2 - 36x - 13}{(x-2)^2}$$
26. Find the maximum profit that a company can make, if the profit function is given by $p(x) = 40 - 20x - 12x^2$.
$$\text{max. Prof.} = 15.1$$
27. The revenue function is $R = 14x - x^2$ and the cost function is $T = x(x^2 - 2)$. Find the marginal functions.
$$MR = 14 - 2x \quad MC = 3x^2 - 2$$
28. What are the properties to be satisfied by an index number ? Verify that Fisher's index number satisfies the properties.
29. Explain about vital statistics and vital records.
30. Distinguish between NRR and GRR.
31. Describe the terms mutually exclusive events and independence of events. Give examples for each of them.
32. If a card is drawn from a pack of playing cards, then find the probability of getting a (i) spade, (ii) king or queen.
$$P(\text{spade}) = \frac{1}{4} \quad P(\text{K or Q}) = \frac{1}{2}$$

(6 × 5 = 30 marks)

Part D (Essay Questions)

Answer any two questions.

33. Given a firms demand function $x = 90 + 2p$ and its cost function $AC = x^3 - 8x^2 + 57x + 2$. Find the level of output which (i) maximizes total revenue, (ii) minimizes marginal costs ; and (iii) maximizes profit.

Profit function

$$x = 45 \text{ when } R \text{ is max.} \quad \frac{dx}{dp} =$$

$$MC = 3x^2 - 2x^2 + 114x + 2 \quad 4x^3 - 24x^2 + 115x + 2$$

Turn over

34. Calculate Fisher's index number from the following data and check whether Fishers ideal index number satisfies all the tests

Commodities	1980		1990		$\sqrt{P_0 P_1}$
	Price	Quantity	Price	Quantity	
A	5	50	6	54	$\sqrt{5 \times 6} = \sqrt{30}$
B	8	16	8	20	$\sqrt{8 \times 8} = \sqrt{64}$
C	3	30	4	32	$\sqrt{3 \times 4} = \sqrt{12}$
D	10	40	12	60	$\sqrt{10 \times 12} = \sqrt{120}$
E	12	60	15	96	$\sqrt{12 \times 15} = \sqrt{180}$

35. Calculate (i) GFR, (ii) SFR, (iii) TFR and (iv) general reproduction rate from the following data :

Age group of child bearing females } : 15 - 19 20 - 24 25 - 29 30 - 34 35 - 39 40 - 44 45 - 49

Number of women ('000) } : 16 16.4 15.8 15.2 14.8 15 14.5

Total births : 260 2244 1894 1320 916 280 145
 $SFR_{in\ each\ age\ group} = \frac{\text{Total births}}{\text{Number of women}} = 0.016 \quad 0.137 \quad 0.119 \quad 0.087 \quad 0.06 \quad 0.02 \quad 0.01$

36. A bag contains 4 white balls, 3 red balls and 3 blue balls. Three balls are drawn at random. Find the probability that the drawn balls are (i) 2 white and a blue ball, (ii) at least one ball of each colour.

$$(1) \frac{4C_2 \times 3C_1}{10C_3} = \frac{1}{20} \quad (2 \times 12 = 24 \text{ marks})$$

$$GFR = \sum (SFR)^k \times C_k$$

$$(2) \frac{4C_1 \times 3C_1 \times 3C_1}{10C_3} = \frac{1}{3} \quad SFR^1 = \frac{1}{2} (SFR)$$

$$\therefore SFR = 0.449$$

$$\sum (SFR)^k \times C_k = \frac{1}{2} \times 0.449 \times 3 = 0.673$$

$$SFR^1 = \frac{\text{Live female birth}}{\text{Female population}}$$

Proportion of female birth = $\frac{1}{2}$.